

Expected Pruning

time limit per test: 2 seconds (4 seconds for Python)
memory limit per test: 250 megabytes
input: standard input
output: standard output
points: 100 · problem code: expectedpruning

You are given a tree with n vertices, rooted at vertex 1.

The following process is repeated until the tree is empty. Let S be the set of vertices that still remain. Choose a vertex v uniformly at random from S , and delete the entire subtree of v (including v itself) from the remaining tree.

Let X be the number of vertices chosen during the process. Output the expected value of X .

It can be shown that the answer can be expressed as a rational number P/Q in lowest terms with Q coprime to $10^9 + 7$. Output $P \cdot Q^{-1} \bmod (10^9 + 7)$.

Input

The first line contains an integer n .

Each of the next $n - 1$ lines contains two integers u and v , describing an undirected edge of the tree.

Vertices are numbered 1 through n . Vertex 1 is the root. If $n = 1$, there are no edge lines.

Output

Print a single integer: the expected number of selections modulo $10^9 + 7$.

Constraints

- $1 \leq n \leq 10^5$
- $1 \leq u, v \leq n$
- The edges form a tree.

Example 1

Input

```
3
1 2
2 3
```

Output

```
833333341
```

Explanation

Root 1 has depth 0, vertex 2 has depth 1, and vertex 3 has depth 2. The expected number of selections is $1 + 1/2 + 1/3 = 11/6$, and $11 \cdot 6^{-1} \equiv 833333341 \pmod{10^9 + 7}$.

These events are strongly dependent: if the root is chosen first, nothing else is ever chosen. Linearity still gives the correct expectation.

Example 2

Input

```
4
1 2
1 3
1 4
```

Output

500000006

Explanation

The root contributes 1, and each of the three leaves contributes $1/2$, for a total of $5/2$.

Example 3

Input

1

Output

1

Explanation

The single vertex is always chosen.